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Last Time: Diagonalization of metrices.
Algoritani Let M be square matrix.
 ( Chracteristic Poly PM(x) = det (M-XI)
  € Solve Pn(1) for eigenvalues.
 (3) Build a basis for R" (or th) of eigenvalues (Eigenbasis).

L) Couple bases of each Eigenspace.
  (4) sprosy each eigenvalle I has geom mit = alg mult,
           the result of these computations is a basis E.
  (5) Realize M = PDP-1 where P=[E] = Rep_E, En (id),
         and D = [1.0] is the watrix of eigenvalues.
Exi We diagondize M = \begin{bmatrix} -9 & -4 \\ 24 & 11 \end{bmatrix}.
                                                                                  If M is nxm
                                                                                 and M has
Char Poly: P_{M}(\lambda) = det(M-\lambda I) = det\begin{bmatrix} -9-\lambda \\ 24 \end{bmatrix}
                                                                                 n district
e-values, then
M is diag'ble.
                            = (-9-\lambda)(11-\lambda) - 24(-4)
                           = -99 -22 +22 +96
                           = \lambda^2 - 2\lambda - 3 = (\lambda - 3)(\lambda + 1)
    = (3-\lambda)(-1-\lambda)

:. We have eigenvalues \lambda_1 = 3 and \lambda_2 = -1
   (NB: Have 2 distant e-values for this 2x2 matrix,) so M is automotically diagonalizable !!).
   \lambda_1 = 3: V_{\lambda_1} = n \cdot ll \left( M - \lambda_1 I \right) = n \cdot ll \left( \frac{-9 - 3}{24} - \frac{4}{11 - 3} \right) = n \cdot ll \left( \frac{-12}{24} - \frac{4}{8} \right)
                                      = n \cdot \left| \begin{bmatrix} 3 & 1 \\ 3 & 1 \end{bmatrix} \right| = n \cdot \left| \begin{bmatrix} 3 & 1 \\ 0 & 0 \end{bmatrix} \right|
     [y] \in V_{\lambda_1} \text{ iff } 3x + y = 0 \text{ iff } y = -3x 
                       B_{\lambda} = \{ \begin{bmatrix} -3 \end{bmatrix} \} \text{ is a basis of } V_{\lambda} .
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$$\frac{\lambda_{2}-1}{\lambda_{1}} \cdot V_{\lambda_{1}} = n \text{ of } \left[\frac{\lambda_{1}}{2\eta} - \frac{\eta}{\|\eta\|}\right] = n \text{ of } \left[\frac{\lambda_{2}}{2\eta} - \frac{\eta}{\|\eta\|}\right] = n \text$$

$$V_{\lambda_{1}} \Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} \text{ iff } \begin{cases} x \\ y - z = 0 \end{cases} \text{ iff } \begin{cases} x = 2t \\ y = t \end{cases} \text{ iff } \begin{bmatrix} x \\ y = t \end{bmatrix} \end{cases}$$

$$= B_{\lambda_{1}} = \begin{bmatrix} 1 \\ 2 \end{bmatrix} \end{bmatrix} \text{ is a basis of } V_{\lambda_{2}}.$$

$$Eigenboss : E = B_{\lambda_{1}} \cup B_{\lambda_{2}} = \begin{bmatrix} 1 \\ 2 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \end{bmatrix} \end{bmatrix} \text{ is a basis of } \mathbb{R}^{3},$$

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